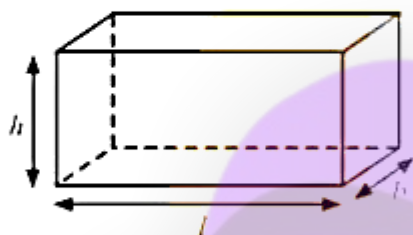


Surface Areas and Volumes

- **Surface areas of cuboid:**



Lateral surface area of the cuboid = $2h(l + b)$

Total surface area of the cuboid = $2(lb + bh + hl)$

Note: Length of the diagonal of a cuboid = $\sqrt{l^2 + b^2 + h^2}$

Example: Find the edge of a cube whose surface area is 294 m^2 .

Solution: Let the edge of the given cube be a .

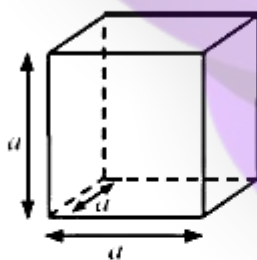
\therefore Surface area of the cube = $6a^2$

Given, $6a^2 = 294$

$\Rightarrow a^2 = 49 \text{ m}^2$

$\therefore a = \sqrt{49} \text{ m} = 7 \text{ m}$

- **Surface areas of cube:**



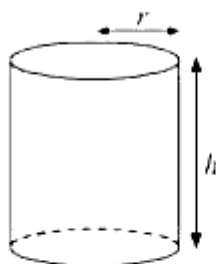
Lateral surface area of the cube = $4a^2$

Total surface area of the cube = $6a^2$

Note: Length of the diagonal of a cube = $\sqrt{a^2 + a^2 + a^2} = \sqrt{3a^2} = \sqrt{3}a$

- **Surface areas of solid cylinder**

- Curved surface area = $2\pi rh$, where r and h are the radius and height
- Total surface area = $2\pi r(r + h)$, where r and h are the radius and height

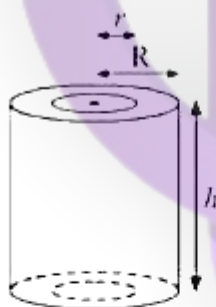


Example : What is the curved surface area of a cylinder of radius 2 cm and height 14 cm?

Solution: Curved surface area of cylinder = $2\pi rh$
 $= 2 \times \frac{22}{7} \times 2 \times 14 \text{ cm}^2$
 $= 176 \text{ cm}^2$

- **Surface areas of hollow cylinder**

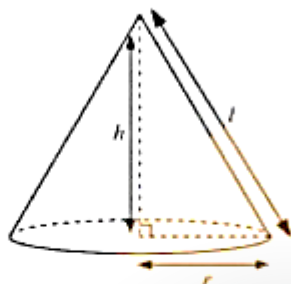
- Curved surface area = $2\pi h (r + R)$, where r, R and h are the inner radius, outer radius and height
- Total surface area = CSA of outer cylinder + CSA of inner cylinder + $2 \times$ Area of base
 $= 2\pi (r + R) (h + R - r)$, where r, R and h are the inner radius, outer radius and height



- **Surface areas of cone**

- Curved surface area = πrl , where r and l are the radius and slant height
- Total surface area = $\pi r (l + r)$, where r and l are the radius and slant height

Here, $l = \sqrt{h^2 + r^2}$, where h is the height.



Example: Calculate the curved surface area of a cone of base radius 3 cm and height 4 cm.

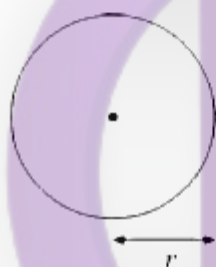
Solution: Here, $r = 3$ cm and $h = 4$ cm

$$\therefore l = \sqrt{h^2 + r^2} = \sqrt{4^2 + 3^2} \text{ m} = 5 \text{ cm}$$

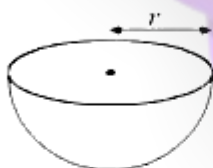
$$\text{Curved surface area} = \pi r l = \pi \times 3 \times 5 \text{ cm}^2 = 15\pi \text{ cm}^2$$

- **Surface areas of sphere and hemisphere**

- Surface area of sphere = $4\pi r^2$, where r is the radius



- Curved surface area of hemisphere = $2\pi r^2$, where r is the radius
- Total surface area of hemisphere = $3\pi r^2$, where r is the radius



Example: What is the radius of a balloon whose surface area is 5544 cm^2 ?

Solution: Let radius of the balloon be r .

$$\text{Surface area of the balloon} = 4\pi r^2 = 5544 \text{ cm}^2$$

$$\Rightarrow 4 \times \frac{22}{7} \times r^2 = 5544 \text{ cm}^2$$

$$\Rightarrow r^2 = \frac{5544 \times 7}{88} \text{ cm}^2$$

$$\Rightarrow r^2 = 441 \text{ cm}^2$$

$$\Rightarrow r = \sqrt{441} = 21 \text{ cm}$$

Thus, the radius of the balloon is 21 cm.

- **Volume of cube and cuboid**

- Volume of cube = a^3 , where a is the side of the cube
- Volume of cuboid = $l \times b \times h$, where l , b and h are respectively the length, breadth and height of the cuboid.

Example: What is the side of a cube of volume 512 cm^3 ?

Solution: Volume of cube = 512 cm^3

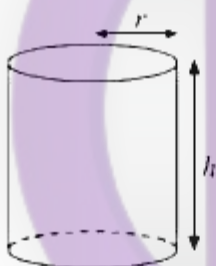
$$\Rightarrow a^3 = 512 \text{ cm}^3$$

$$\Rightarrow a = \sqrt[3]{512 \text{ cm}^3}$$

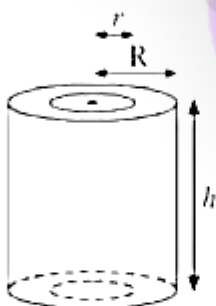
$$\Rightarrow a = 8 \text{ cm}$$

- **Volume of the solid cylinder and hollow cylinder**

- Volume of solid cylinder = $\pi r^2 h$, where r and h are the radius and height of the solid cylinder



- Volume of the hollow cylinder = $\pi (R^2 - r^2) h$, where r , R and h are the inner radius, outer radius and height of hollow cylinder



Example: Find the volume of the pillar of radius 70 cm and height 10 m.

Solution: Radius of the pillar (r) = $70 \text{ cm} = \frac{70 \text{ m}}{100} = 0.7 \text{ m}$

Height of the pillar (h) = 10 m

$$\begin{aligned}\text{Volume of the pillar} &= \pi r^2 h \\ &= \frac{22}{7} \times (0.7)^2 \times 10 \text{ m}^3 \\ &= 15.4 \text{ m}^3\end{aligned}$$

- **Volume of a cone** = $\frac{1}{3} \pi r^2 h$, where r and h are the radius of base and height of the cone.

Example: Calculate the volume of a cone of base radius 3 cm and height 4 cm.

Solution: Here, $r = 3$ cm and $h = 4$ cm

$$\begin{aligned}\text{Volume} &= \frac{1}{3} \pi r^2 h \\ &= \frac{1}{3} \times \pi \times 3 \text{ cm} \times 3 \text{ cm} \times 4 \text{ cm} \\ &= 12\pi \text{ cm}^3\end{aligned}$$

- **Volume of sphere and hemisphere**

$$\begin{aligned}\text{Volume of sphere} &= \frac{4}{3} \pi r^3 \\ \text{Volume of hemisphere} &= \frac{2}{3} \pi r^3\end{aligned}$$

Example 1: Calculate the volume of a sphere whose surface area is $9\pi \text{ cm}^2$.

Solution: Surface area = $9\pi \text{ cm}^2$

$$\Rightarrow 4\pi r^2 = 9\pi$$

$$\Rightarrow r^2 = \frac{9}{4}$$

$$\Rightarrow r = \frac{3}{2} \text{ cm}$$

$$\text{Volume of sphere} = \frac{4}{3} \pi r^3 = \frac{4}{3} \pi \left(\frac{3}{2} \text{ cm}\right)^3 = \frac{4}{3} \pi \left(\frac{27}{8}\right) \text{ cm}^3 = 4.5\pi \text{ cm}^3$$

Example 2: The inner radius of a hemispherical bowl is 4.2 cm. What is the capacity of the bowl?

Solution: Here, $r = 4.2$ cm

$$\text{Volume of the bowl} = \frac{2}{3} \pi r^3 = \frac{2}{3} \times \frac{22}{7} \times (4.2 \text{ cm})^3 = 155.232 \text{ cm}^3$$

$$1 \text{ ml} = 1 \text{ cm}^3$$

Thus, the capacity of the bowl is 155.232 ml.